

# Semi-partitioned Model on Dual-core Mixed Criticality System



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# Background

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- Mixed Criticality System
  - Task has different Worst Case Execution Time (C) for different criticality levels (L)
  - For the same task:  
$$L_m > L_n \Rightarrow C_m > C_n$$
- Two criticality levels (HI, LO)
  - HI > LO



# Background

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- Vestal's Approach<sup>[1]</sup>
  - All tasks keeps schedulable
  - Pessimistic
- Runtime monitors
  - LO-crit task -> prevent from execution
  - HI-crit task -> mode change
- AMC<sup>[2]</sup> and EDF-VD<sup>[3]</sup> etc.

[1] S. Vestal. Preemptive scheduling of multi-criticality systems with varying degrees of execution time assurance. In *Real-Time Systems Symposium, 2007. RTSS 2007. 28th IEEE International*, pages 239–243. IEEE, 2007.

[2] S. K. Baruah, A. Burns, and R. I. Davis. Response-time analysis for mixed criticality systems. In *Real-Time Systems Symposium*, pages 34–43. IEEE, 2011.

[3] S. Baruah, H. Li, and L. Stougie. Towards the design of certifiable mixed-criticality systems. In *Real-Time and Embedded Technology and Applications Symposium (RTAS)*, pages 13–22. IEEE, 2010.



# Motivation

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- Explore a way that all of the tasks remain schedulable throughout the criticality level changes.
- Multi-core platform provides the option of migration

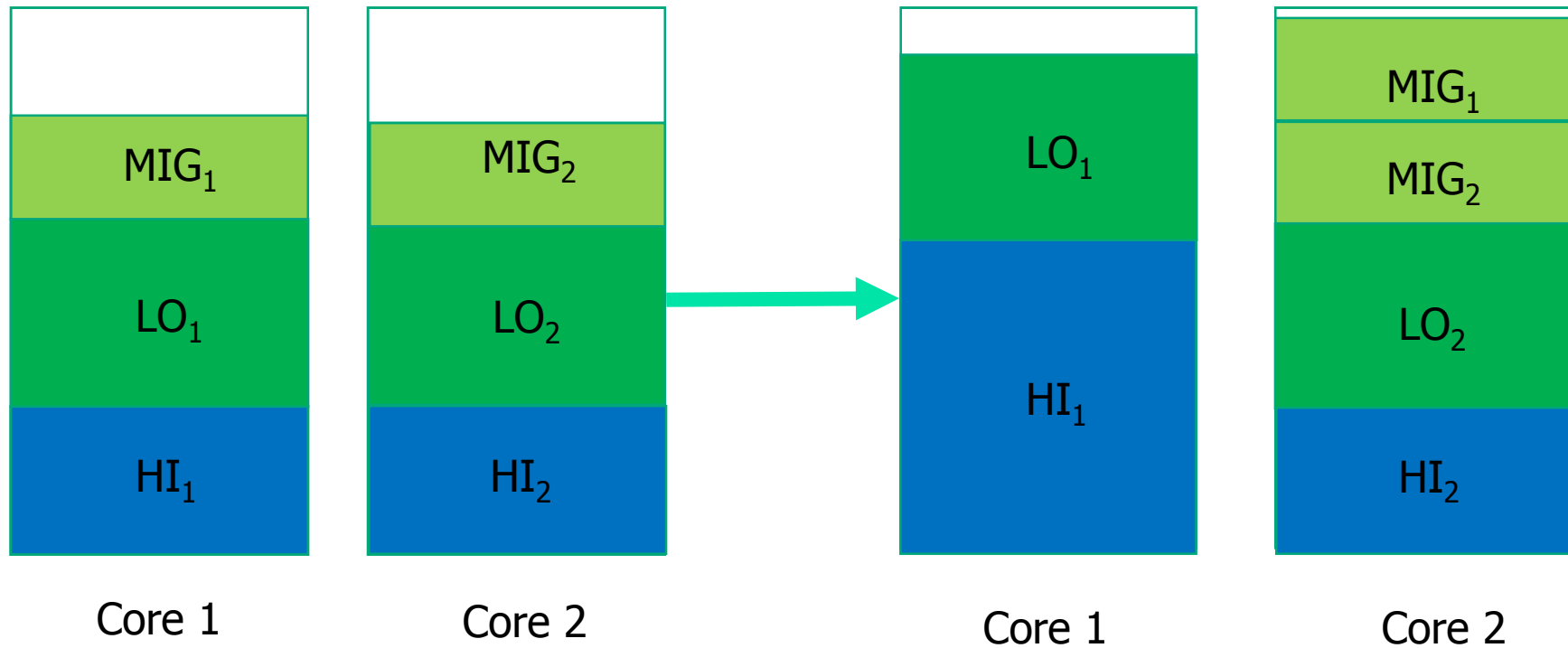


# Assumptions

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- Independent tasks
- Deadline < period
- Migration cost
- Mode change frequency and isolation

# Semi-partitioned Model





# Semi-partitioned Model

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- If all tasks execute within their LO-crit budget then all deadlines are met and no tasks migrate.
- No LO-crit task is allowed to exceed its LO-crit budget.
- If HI-crit tasks on one core exceed their LO-crit budget, then some LO-crit tasks will migrate, but ALL LO-crit tasks and HI-crit tasks remain schedulable.
- If HI-crit tasks on more than one core exceed their LO-crit budget, then some LO-crit tasks will be abandoned, but all HI-crit tasks remain schedulable (without migration).



# State View

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- Task set  $S$  to represent the collection of all tasks sets:
  - $S = (LO_1 \cup LO_2) \cup (HI_1 \cup HI_2) \cup (MIG_1 \cup MIG_2)$
- State  $X$  to represent the normal execution state:
  - $X_1 = LO_1 \cup HI_1 \cup MIG_1$
  - $X_2 = LO_2 \cup HI_2 \cup MIG_2$
  - $S = X_1 \cup X_2$

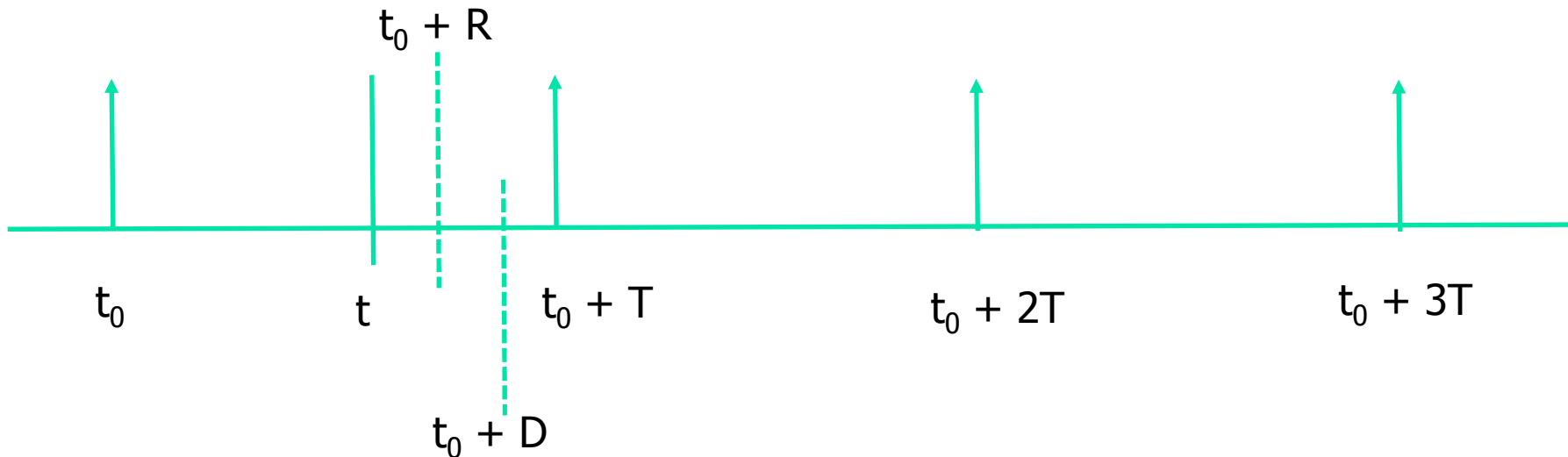


# One core enters HI-crit Mode

- State  $Y(1)$  to represent the state that Core  $c_1$  enters HI-crit mode.
  - $Y(1)_1 = LO_1 \cup HI_1$
  - $Y(1)_2 = LO_2 \cup HI_2 \cup MIG_1 \cup MIG_2$
  - $S = Y(1)_1 \cup Y(1)_2$
- Release Jitter and Reduced deadline issues for migrating tasks ( $MIG_1$ )

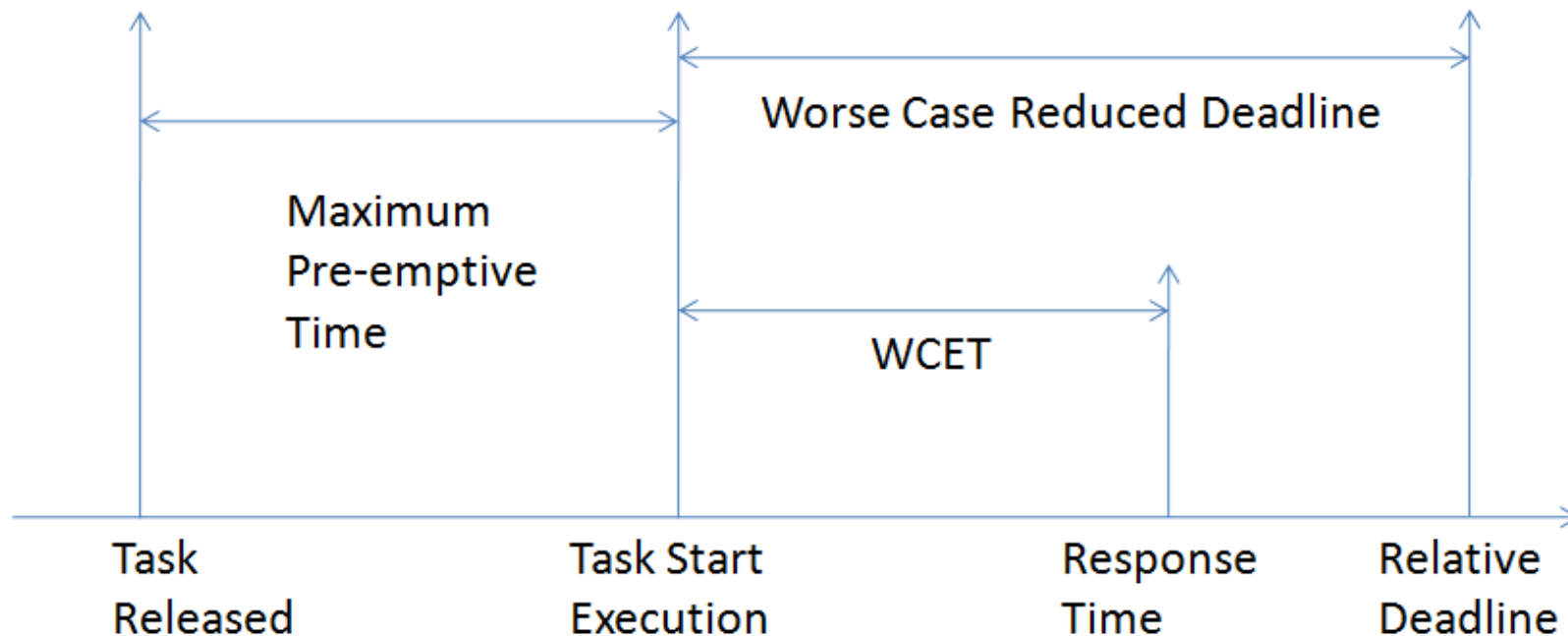
# Release Jitter Issue

- Task released at time  $t_0$  and migrates at time  $t$



# Reduced Deadline Issue

$$d'_{i \max} = d_i - (R_i(\text{LO}) - C_i)$$



# Both Cores in HI-crit Mode (1)

- $BY(1)$  to represent the case that core  $c_2$  also enters HI-crit mode from state  $Y(1)$ 
  - $BY(1)_1 = LO_1 \cup HI_1$
  - $BY(1)_2 = HI_2$
  - $S = BY(1)_1 \cup BY(1)_2 \cup LO_2 \cup MIG_1 \cup MIG_2$

# Both Cores in HI-crit Mode (2)

- $BX$  to represent the case that both cores enter HI-crit mode at the same time.
  - $BX1 = LO_1 \cup HI_1$
  - $BX2 = LO_2 \cup HI_2$
  - $S = BX_1 \cup BX_2 \cup MIG_1 \cup MIG_2$



# Allocation

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- Bin packing algorithms
  - Criticality aware utilisation decreasing  
g
- Non-migration
- Migration



# Choice of Migration

- Regarding to the equation:

- Migrating LO-crit tasks with largest slack time

$$\forall \tau_i \in (Y(1)_1 \cup Y(2)_2) :$$

$$R_i(HI)^* = C_i(L_i)$$

$$+ \sum_{j \in \text{chp}H(i)} \left\lceil \frac{R_i(HI)^*}{T_j} \right\rceil C_j(HI)$$

$$+ \sum_{k \in \text{chp}L(i)} \left\lceil \frac{R_i(HI)^*}{T_k} \right\rceil C_k(LO)$$

$$+ \sum_{l \in \text{chp}MIG(i)} \left\lceil \frac{R_i(LO)}{T_l} \right\rceil C_l(LO)$$

- Schedulability issues after migration

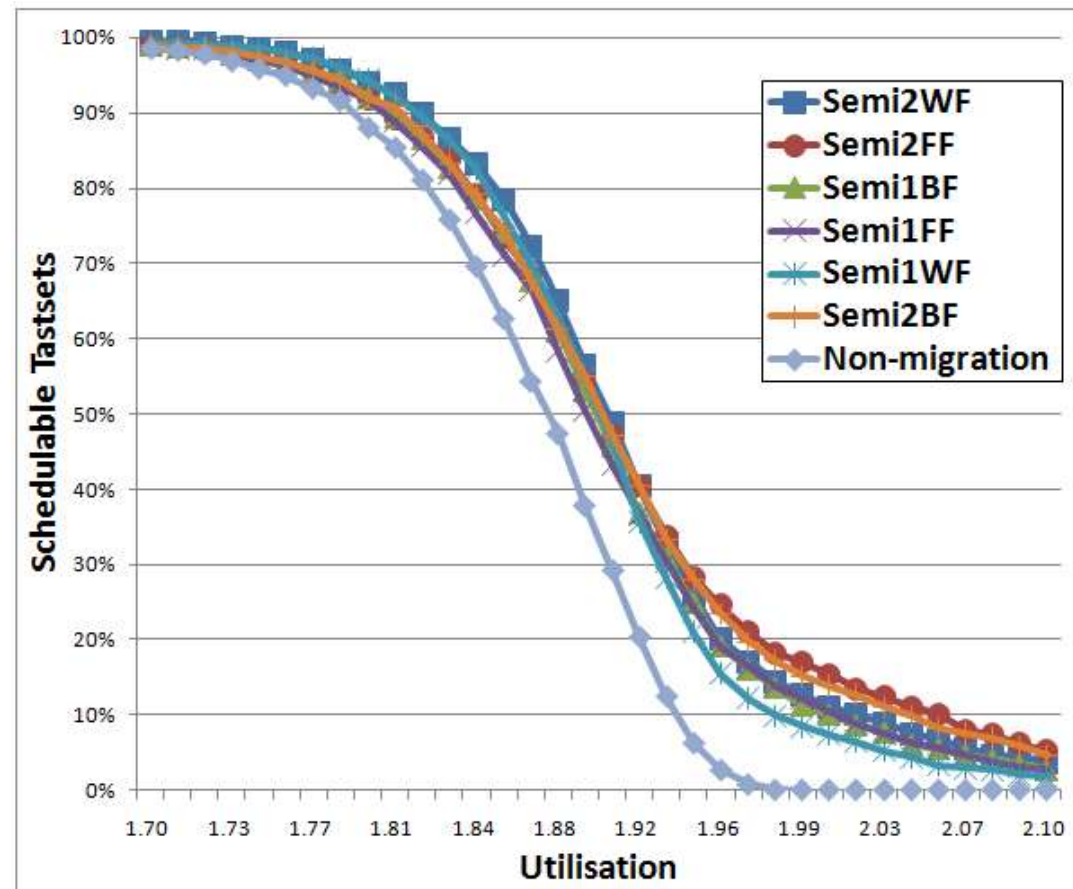
# Semi-partitioned Model Configuration

- Two approaches on deciding migrating tasks
  - Semi1: task fetched
  - Semi2: task assigned
- Three bin-packing algorithms
  - FF, BF, WF
- Audeslay's priority assignment



# Evaluation

- $f = 3$
- $P = 0.5$
- $n = 12$
- $ts = 10000$





# Evaluation

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- Weighted graphs
  - Taskset size
  - Percentage of HI-crit tasks
  - Factor of WCET differences
- All algorithms behave better than the non-migration algorithm
- Semi2WF and Semi2FF



# Conclusion

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- Semi-partitioned model
- Six possible approaches
- Suggestion
- Future Work